| Department of Mathematics |  |  |  |  | CLASS: I B.Sc. Mathematics |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Semester | Course <br> Type | Course Code | Course <br> Title | Credits | Contact <br> Hours/ <br> week | CIA | Ext | Total |
| II | Core | 20U2MMC3 | Analytical <br> Geometry of Three <br> Dimension and <br> Vector Calculus | 4 | 4 | 25 | 75 | 100 |

## COURSE OBJECTIVES:

1. Acquire a knowledge of geometry of spheres, cone, cylinder in 3 Dimensional problems.
2. Apply analytical techniques in solving 3D problems.
3. Demonstrate an understanding in vector differentiation.
4. Knowledge of evaluating line and surface integrals by applying Green's, Gauss and Stoke's theorems.

## Unit-I:

Equation of a Plane - passing through three points - coplanar - intercept form - Normal form - Angle between two planes - parallel planes - perpendicular planes - intersection of two planes - Angle bisectors of two planes

## Unit-II:

Introduction -Equation of a sphere - centre radius form - general form - diameter form - Tangent line and tangent plane - tangent plane parallel to plane -tangent plane passes through a point- intersection of two spheres - Section of a sphere - orthogonal.

## Unit-III:

Equation of a Cone - Right circular cone - Angle between line of intersection of cone and a plane - Cylinder Right circular cylinder - circular cylinder.

## Unit-IV:

Vector point function - Scalar point function - Derivative of a vector and derivative of a sum of vectors Derivative of a product of a scalar and a vector point function - Derivative of a scalar product and vector product - The vector operator 'del' - Gradient of a scalar point function - Divergence of a vector - Curl of a vector - solenoidal and irrotational vectors - Laplacian operator.

## Unit-V:

Line integrals - Surface integrals - Green's, Gauss and Stoke's theorems (without proof) - Problems.

## Text Book:

1. S. Arumugam, A.Thangapandi Issac \& Somasundaram, Analytical, Edition 20, Yes Dee Publishing Private Limited, Chennai.
Chapters:-10,12, 13(Analytical Geoemetry)
2. S. Arumugam \&A.Thangapandi Issac, Analytical Geometry (3D) and Vector Calculus, Edition 2017, New Gamma Publishing House.
Part B (Vector Calculus) -Chapters: 5,6,7

## Reference Books:

1. T. K. Manickavachagom Pillai and T. Natarajan, Analytical Geometry (3D), Edition 2011, S. Viswanathan (Printers \& Publishers) Pvt. Ltd.
2. M. K.Venkataraman and Manorama Sridhar, Vector calculus and Fourier series, 2002 Edition, The National Publishing Company.

## Web References:

1. https://nptel.ac.in/courses/111/105/111105122/
2. https://www.maths.ox.ac.uk/study-here/undergraduate-study/practice-problems
3. http://www.freebookcentre.net/SpecialCat/Free-Mathematics-Books-Download.html

## Course Learning Outcomes

On the successful completion of the course, students will be able to

| Number | Course Learning Outcome | Knowledge <br> level |
| :--- | :--- | :---: |
| CLO1 | Understand the basic concept of plane. Compute angles between two <br> planes and bisectors of two planes. <br> Understand the basic concept of sphere. | Upto K3 |
| CLO2 | Know the concept of sphere - Evaluate tangent line and tangent plane and <br> section of sphere. | Upto K4 |
| CLO3 | Obtain the geometrical knowledge of cone and Cylinder. Determine <br> equations of cone, right cone, cylinder and right circular cylinder. | Upto K3 |
| CLO4 | Acquire the idea of gradient, divergence, curl, solenodial and irrational of <br> vectors. Use vector differentiation in solving problems | Upto K2 |
| CLO5 | Discuss about green's, Stoke's, Gauss Divergence theorem and apply it in <br> solving various problems. | Upto K4 |

K1- Recall, K2 - Understanding, K3 - Applying, K4- analyzing, K5-Evaluating, K6-Creating

## Mapping with Courses Learning Outcomes (CLOs)

|  | O | No | O | $\underset{Q}{0}$ | $\stackrel{\pi}{2}$ | $$ | $\begin{aligned} & \text { N } \\ & \text { On } \\ & \text { O } \end{aligned}$ | $\begin{aligned} & \text { n } \\ & \text { Nan } \end{aligned}$ | $\begin{aligned} & \text { J } \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { 世o } \\ & 0 \\ & \end{aligned}$ | $\begin{aligned} & \text { O} \\ & \text { O} \\ & \text { Nan } \end{aligned}$ | $\begin{aligned} & \hat{O} \\ & \hat{0} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CLO1 | 2 | 1 | - | - | - | 3 | 3 | 3 | 1 | - | - | - |
| CLO2 | 1 | 2 | - | - | 1 | 3 | 3 | 3 | 3 | 1 | 2 | 1 |
| CLO3 | 1 | 2 | - | - | 1 | 3 | 3 | 3 | 3 | - | 2 | 1 |
| CLO4 | 3 | - | - | 1 | - | 3 | 2 | 3 | 2 | 1 | - | 1 |
| CLO5 | 2 | 3 | - | 1 | 2 | 3 | 1 | 2 | 3 | - | 3 | - |

## Pedagogy:

Lecture, Power point presentation, Group Discussion, Seminar, Quiz, Problem Solving and Tutorial.

## Lesson Plan

| S. No. | UNIT | DESCRIPTION | TAKING HOURS | TOTAL | Pedagogy |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | I | Equation of a Plane and its problem | 4 | 12 | Lecture, Quiz |
|  |  | Angle between two planes and examples | 4 |  | Lecture |
|  |  | Angle bisectors of two planes and problems | 4 |  | Lecture ,Problem Solving |
| 2. | II | Introduction to sphere | 1 | 12 | Lecture ,Group Discussion |
|  |  | Equation of a sphere | 3 |  | Lecture ,Problem Solving |
|  |  | Tangent line and tangent plane | 4 |  | Lecture, quiz |
|  |  | Section of a sphere and its problems | 4 |  | Lecture, Tutorial |
| 3. | III | Equation of a Cone | 2 | 12 | Lecture |
|  |  | Cone with Vertex at the origin | 2 |  | Lecture, Quiz |
|  |  | Right circular cone and it's problems | 3 |  | Lecture |
|  |  | Equation of cylinder | 2 |  | Lecture, Group Discussion |
|  |  | Right circular cylinder and it's problems | 3 |  | Lecture, Tutorial |
| 4. | IV | Vector point function - Scalar point function - examples | 1 | 12 | Lecture, Quiz |
|  |  | Derivative of a vector and derivative of a sum of vectors | 1 |  | Lecture |
|  |  | Derivative of a product of a scalar and a vector point function | 1 |  | Lecture |
|  |  | Derivative of a scalar product and vector product | 2 |  | Lecture, ICT |
|  |  | The vector operator 'del' | 1 |  | Lecture, Group discussion |
|  |  | Gradient of a scalar point function | 2 |  | Lecture |
|  |  | Divergence of a vector | 1 |  | Lecture |
|  |  | Curl of a vector - solenoidal and irrotational vectors | 1 |  | Lecture, problem solving |
|  |  | Laplacian operator. | 2 |  | Lecture |
| 5. | V | Line integral and Surface integral | 2 | 12 | Lecture, Quiz |
|  |  | Volume integral- example | 2 |  | Lecture, ICT |
|  |  | Stokes Theorem, Gauss-divergence Theorem -problems | 4 |  | Lecture, Seminar |
|  |  | Green's Theorem in two dimensions <br> - Problems | 4 |  | Lecture ,Tutorial. |
|  |  | Total |  | 60 |  |

Course Designer: Dr. I. Padmavathi, Assistant Professor of Mathematics

